Functions

1. If
$$f(x) = x^3 + 4x - 3$$
, find $f(1), f(-1), f(0), f(\sqrt{2})$

2. Sketch the graph and determine the domain and range of f

a)
$$f(x) = -4x + 3$$

b)
$$f(x) = 3$$

c)
$$f(x) = \sqrt{36 - x^2}$$

d)
$$f(x) = \sqrt{x^2 - 49}$$

$$e) \quad f(x) = \frac{1}{x-4}$$

f)
$$f(x) = \frac{5}{x^2 - x - 12}$$

g)
$$f(x) = |x - 4|$$

h)
$$f(x) = 2 - \sqrt{x}$$

3. Find the sum, difference and product of f and g

a)
$$f(x) = 3x^2, g(x) = \frac{1}{2x - 3}$$
 b) $f(x) = x^3 + 3x, g(x) = 3x^2 + 1$

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$$f(x) = x^3 + 3x, g(x) = 3x^2 + 1$$

c)
$$f(x) = 2x^3 - x + 5, g(x) = x^2 + x + 2$$

4. Find $(f \circ g)(x)$ and $(g \circ f)(x)$ where $(f \circ g)(x) = f(g(x))$

a)
$$f(x) = 2x^2 + 5$$
, $g(x) = 4 - 7x$ b) $f(x) = \sqrt{2x + 1}$, $g(x) = x^2 + 3$

b)
$$f(x) = \sqrt{2x+1}, g(x) = x^2 + 3$$

c)
$$f(x) = 2x - 3$$
, $g(x) = \frac{x+3}{2}$

5. Graph the following functions and determine the value of y as x gets close to the indicated value.

b)
$$f(x) = \frac{x-4}{x^2 - x - 12}$$
 as x gets close to 4 b) $f(x) = \frac{x^3 - 27}{x^2 - 9}$ as x gets close to 3

c)
$$f(x) = \frac{4-x^2}{3-\sqrt{x+5}}$$
 as x gets close to 2 d) $f(x) = \frac{3x-2}{9x+7}$ as x gets close to ∞

e)
$$f(x) = \frac{2x^3}{x^2 + 1}$$
 as x gets close to ∞